## Bayesian large-scale structure inference and cosmic web analysis

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#### The big picture: the Universe is highly structured

You are here. Make the best of it...



How did structure appear in the Universe?

A joint problem!

- How did the Universe begin?
  - What are the statistical properties of the initial conditions?
- How did the large-scale structure take shape?
  - What is the physics of dark matter and dark energy?

#### We have theoretical and computer models...

• Initial conditions: a Gaussian random field

$$\mathcal{P}(\delta^{\mathbf{i}}|S) = \frac{1}{\sqrt{|2\pi S|}} \exp\left(-\frac{1}{2}\sum_{x,x'}\delta^{\mathbf{i}}_{x}S^{-1}_{xx'}\delta^{\mathbf{i}}_{x'}\right)$$

Everything seems consistent with the simplest inflationary scenario, as tested by Planck.



Planck 2015 XX, arXiv:1502.02114

 Structure formation: numerical solution of the Vlasov-Poisson system for dark matter dynamics

$$\frac{\partial f}{\partial \tau} + \frac{\mathbf{p}}{ma} \cdot \nabla f - ma \nabla \Phi \cdot \frac{\partial f}{\partial \mathbf{p}} = 0$$
$$\Delta \Phi = 4\pi \mathbf{G} a^2 \bar{\rho} \delta$$

Y. Dubois & S. Colombi (IAP)

#### But some questions remain

- 1. How do we **test** these frameworks?
  - Usually the two problems of initial conditions and structure formation are addressed in isolation.
  - Ideally, galaxy surveys should be analyzed in terms of the joint constraints that they place on these two questions.

2. How did this happen in **Our** Universe?

### 1. How do we test our models?



Redshift Volume  $N_{
m modes}$  $k_{
m max}$  $(Gpc^3)$  $({
m Mpc}/h)^{-1}$ range  $10^{7}$ 0-1 50 0.15 1-2 0.5 5x10<sup>8</sup> 140 1010 2-3 160 1.3

M. Zaldarriaga

Precise tests require many

J. Cham – PhD comics

- modes.
- In 3D galaxy surveys, the number of modes usable scales as  $k_{\rm max}^3$ .



- The challenge: non-linear evolution at small scales and late times.
- per The strategy:
  - Pushing down the smallest scale usable for cosmological analysis
  - Inferring the initial conditions from galaxy positions

In other words: go beyond the linear and static analysis of the LSS.

## 2. How did this happen in our Universe?

This means that we cannot do, for example:



 Standard analyses: reduce the data to some statistics, then fit some model parameters

- We have to do a joint analysis of all aspects, including density reconstruction
  - Provides powerful constraints
  - Propagates uncertainties between all parts of the analysis
  - Avoids using the data twice
- It is a process known as data assimilation

Can we just fit the entire survey?

## Why Bayesian inference?

- What do we need to fit the entire survey? Inference of signals = ill-posed problem
  - Incomplete observations: finite resolution, survey geometry, selection effects
  - Noise, biases, systematic effects
  - Cosmic variance

#### No unique recovery is possible!

"What is the formation history of the Universe?"





"What is the probability distribution of possible formation histories (signals) compatible with the observations?"

Bayes' theorem:  $\mathcal{P}(s|d)\mathcal{P}(d) = \mathcal{P}(d|s)\mathcal{P}(s)$ 

Cox-Jaynes theorem: Any system to manipulate "*plausibilities*", consistent with Cox's desiderata, is isomorphic to (Bayesian) probability theory



### Bayesian forward modeling: the ideal scenario

Forward model = N-body simulation + Halo occupation + Galaxy formation + Feedback + ...



(intel) inside

#### Bayesian forward modeling: the ideal scenario



#### BORG: Bayesian Origin Reconstruction from Galaxies



What makes the problem tractable:

- Sampler: Hamiltonian Markov Chain Monte Carlo method
- Data model: Gaussian prior Second-order Lagrangian perturbation theory (2LPT) – Poisson likelihood (and also: luminosity-dependent galaxy bias, automatic noise level calibration)



(galaxy catalog + meta-data: selection functions, completeness...)

Jasche & Wandelt 2013, arXiv:1203.3639 Jasche, FL & Wandelt 2015, arXiv:1409.6308 Samples of possible 4D states

#### Chrono-Cosmography

#### BORG at work: SDSS chrono-cosmography



The BORG SDSS run:

334,074 galaxies, ≈ 17 millions parameters, 12,000 samples, 3 TB, 10 months on 32 cores

#### Bayesian chrono-cosmography from SDSS DR7



Data

Jasche, FL & Wandelt 2015, arXiv:1409.6308

#### 14

#### Bayesian chrono-cosmography from SDSS DR7



One sample

Jasche, FL & Wandelt 2015, arXiv:1409.6308

#### Bayesian chrono-cosmography from SDSS DR7



Posterior mean

Jasche, FL & Wandelt 2015, arXiv:1409.6308

#### Evolution of cosmic structure



#### Jasche, FL & Wandelt 2015, arXiv:1409.6308

17

#### The formation history of the Sloan Great Wall



Jasche, Romano-Díaz, FL & Wandelt, in prep.

## THE NON-LINEAR REGIME OF STRUCTURE FORMATION

#### Non-linear filtering via constrained simulations



#### FL, Jasche, Sutter, Hamaus & Wandelt 2014, arXiv:1410.0355

#### Non-linear filtering via constrained simulations



#### FL, Jasche, Sutter, Hamaus & Wandelt 2014, arXiv:1410.0355

21

#### COLA: COmoving Lagrangian Acceleration

- Write the displacement vector as:  $\, {f s} = {f s}_{
m LPT} + {f s}_{
m MC} \,$ 

• Time-stepping (omitted constants and Hubble expansion):



Tassev, Zaldarriaga & Einsenstein 2013, arXiv:1301.0322

Tassev & Zaldarriaga 2012, arXiv:1203.5785

#### Non-linear filtering improves the fit



#### FL, Jasche, Sutter, Hamaus & Wandelt 2014, arXiv:1410.0355

23

## How is the Cosmic Web Woven?

#### Uncertainty quantification



Uncertainty quantification is crucial!



Can we propagate uncertainty quantification to cosmic web analysis?

#### Cosmic web classification procedures

void, sheet, filament, cluster?

• The **T-web**:

uses the sign of  $\mu_1, \mu_2, \mu_3$ : eigenvalues of the tidal field tensor, Hessian of the gravitational potential:  $T_{ij}(\mathbf{x}) = \partial_i \partial_j \Phi(\mathbf{x})$ 

Hahn et al. 2007, arXiv:astro-ph/0610280

#### T-web structures inferred by BORG





FL, Jasche & Wandelt 2015, arXiv:1502.02690

#### T-web structures inferred by BORG

Initial conditions 400



FL, Jasche & Wandelt 2015, arXiv:1502.02690

## Entropy of the structure types posterior $H\left[\mathcal{P}(\mathrm{T}(\vec{x}_k)|d)\right] \equiv -\sum_{i=0}^{3} \mathcal{P}(\mathrm{T}_i(\vec{x}_k)|d) \log_2(\mathcal{P}(\mathrm{T}_i(\vec{x}_k)|d)) \quad \text{in shannons (Sh)}$



Initial conditions



(more to come on the connection between cosmic web analysis and information theory)

#### A decision rule for structure classification

• Space of "input features":

 $\{T_0 = void, T_1 = sheet, T_2 = filament, T_3 = cluster\}$ 

• Space of "actions":

 $\{a_0 = \text{``decide void''}, a_1 = \text{``decide sheet''}, a_2 = \text{``decide filament''}, a_3 = \text{``decide cluster''}, a_{-1} = \text{``do not decide''}\}$ 

A problem of **Bayesian decision theory**: one should take the action which maximizes the utility  $_3$ 

$$U(a_j(\vec{x}_k)|d) = \sum_{i=0} G(a_j|\mathbf{T}_i) \mathcal{P}(\mathbf{T}_i(\vec{x}_k)|d)$$

How to write down the gain functions?



• Without data, the expected utility is

 $U(a_j) = 1 - \alpha$  if  $j \neq 1$  "Playing the game"  $U(a_{-1}) = 0$  "Not playing the game"

- With  $\alpha = 1$ , it's a *fair game*  $\implies$  always play  $\implies$  "speculative map" of the LSS
- Values \alpha > 1 represent an aversion for risk
   increasingly "conservative maps" of the LSS



#### FL, Jasche & Wandelt 2015, arXiv:1503.00730

32

### Inference of the dark matter phase-space sheet

- The dark matter phase-space sheet has been studied so far in simulations
- e.g. Neyrinck 2012, arXiv:1202.3364 Abel, Hahn & Kaehler 2012, arXiv:1111.3944 Shandarin, Habib & Heitmann 2012, arXiv:1111.2366
  - BORG infers Lagrangian
     dynamics in real data
  - This is opening the way to new confrontations between data and theory
  - Identified structures have a direct physical interpretation





#### Cosmic web classification procedures

void, sheet, filament, cluster?

The T-web:

uses the sign of  $\mu_1, \mu_2, \mu_3$ : eigenvalues of the tidal field tensor, Hessian of the gravitational potential:  $T_{ij}(\mathbf{x}) = \partial_i \partial_j \Phi(\mathbf{x})$ 

Hahn et al. 2007, arXiv:astro-ph/0610280

• DIVA:

uses the sign of  $\lambda_1, \lambda_2, \lambda_3$ : eigenvalues of the shear of the Lagrangian displacement field:  $R_{\ell m}(\mathbf{q}) = \partial_m \Psi_\ell(\mathbf{q})$ 

Lavaux & Wandelt 2010, arXiv:0906.4101

• ORIGAMI :

uses the dark matter "phase-space sheet" (number of orthogonal axes along which there is shell-crossing)

Falck, Neyrinck & Szalay 2012, arXiv:1201.2353

Lagrangian classifiers

now usable in real data!

#### **Comparing classifiers**



#### FL, Jasche, Lavaux & Wandelt, in prep.



FL, Lavaux, Jasche & Wandelt, in prep.

#### HINTS FROM THE DARK

#### Dark matter voids: pipeline

Why BORG?

**Sparsity & Bias** 

Sutter *et al.* 2013, arXiv:1309.5087 Sutter *et al.* 2013, arXiv:1311.3301

#### How?

VIDE toolkit: Sutter et al. 2015, arXiv:1406.1191 www.cosmicvoids.net

based on ZOBOV: Neyrinck 2007, arXiv:0712.3049

38



## BORG unveils many more voids

Void number function





## Voids in constrained regions only

Voids are **Poissondominated** objects: 10x more voids require 100x more galaxies!

#### Reduction of statistical uncertainty in voids catalogs

Ellipticity distribution

Radial density profile



All catalogs are publicly available at <u>www.cosmicvoids.net</u> for follow-up projects.

For example, these voids should have an effect on CMB photons...

FL, Jasche, Sutter, Hamaus & Wandelt 2015, arXiv:1410.0355

# How to detect secondary effects in the Cosmic Microwave Background?

#### Producing LSS-CMB observables



#### Templates for secondary effects in the CMB



• The full posterior is available for Hierarchical Bayesian analysis with G. Lavaux, J. Jasche, B. Wandelt

### Summary & concluding thoughts

- A new method for principled analysis of galaxy surveys: Bayesian large-scale structure inference
  - Uncertainty quantification (noise, survey geometry, selection effects and biases)
  - Non-linear and non-Gaussian inference, with improving techniques
- Application to data: four-dimensional chrono-cosmography
  - Simultaneous analysis of the morphology and formation history of the large-scale structure
  - Physical reconstruction of the initial conditions
  - Characterization of the dynamic cosmic web underlying galaxies
  - Inference of cosmic voids at the level of the dark matter field
  - Cross-correlation of galaxy surveys and CMB data through kSZ/iSW/RS effects